# REPORT DOCUMENTATION PAGE

Form Approved OMB NO. 0704-0188

The public reporting burden for this collection of information is estimated to average 1 hour per response, including the time for reviewing instructions, searching existing data sources, gathering and maintaining the data needed, and completing and reviewing the collection of information. Send comments regarding this burden estimate or any other aspect of this collection of information, including suggesstions for reducing this burden, to Washington Headquarters Services, Directorate for Information Operations and Reports, 1215 Jefferson Davis Highway, Suite 1204, Arlington VA, 22202-4302. Respondents should be aware that notwithstanding any other provision of law, no person shall be subject to any oenalty for failing to comply with a collection of information if it does not display a currently valid OMB control number. PLEASE DO NOT RETURN YOUR FORM TO THE ABOVE ADDRESS.

1. REPORT I	DATE (DD-MM-	-YYYY)	2. REPORT TYPE		3. DATES COVERED (From - To)		
03-03-2016	5		Final Report		20-Jun-2014 - 19-Mar-2015		
4. TITLE AN	ND SUBTITLE			5a. C0	5a. CONTRACT NUMBER		
Final Repor	rt: Localizatio	n of Gunfire fi	rom Multiple Shooters	W911	W911NF-14-1-0270		
`	-	2, Information	Processing & Fusion;	5b. Gl	RANT NUMBER		
STIR Progr	ram)						
				5c. PROGRAM ELEMENT NUMBER			
6. AUTHOR	S			5d. PR	5d. PROJECT NUMBER		
Richard J. K	Kozick						
				5e. TA	5e. TASK NUMBER		
				5f. WORK UNIT NUMBER			
7. PERFOR	MING ORGANI	IZATION NAMI	ES AND ADDRESSES	•	8. PERFORMING ORGANIZATION REPORT		
Bucknell U	•				NUMBER		
Bucknell Un 1 Dent Driv	•						
Lewisburg,		1783	7 -2005				
			NAME(S) AND ADDRES	S	10. SPONSOR/MONITOR'S ACRONYM(S)		
(ES)			<b>、</b>		ARO		
U.S. Army Research Office P.O. Box 12211				11. SPONSOR/MONITOR'S REPORT NUMBER(S)			
Research Triangle Park, NC 27709-2211				65977-CS-II.2			
12 DICTRID	12. DISTRIBUTION AVAILIBILITY STATEMENT				03777 C5 11.2		
		Distribution Unl	imited				
13. SUPPLEMENTARY NOTES  The views emissions and/or findings contained in this report are those of the outbox(s) and should not contribute as an official Department.							
The views, opinions and/or findings contained in this report are those of the author(s) and should not contrued as an official Department of the Army position, policy or decision, unless so designated by other documentation.							
-							
14. ABSTRA		dataction syst	rome (SW CDS) are im	aartant far	gituational avvarances because they		
Soldier-wearable gunfire detection systems (SW-GDS) are important for situational awareness because they provide an estimate of the shooter's location and the trajectory of the bullet. Individual SW-GDS units provide an							
estimate of the shooter's location and the trajectory of the buriet. Individual Sw-GDS units provide an estimate of the range and bearing to the shooter for each shot, as well as "raw" data that includes time-of-arrival							
(TOA) and direction-of-arrival (DOA) of the muzzle blast (MB) produced by the weapon and the shock wave (SW)							
produced by the supersonic bullet. The localization accuracy is improved with data fusion between networked SW-							
CDC concernite We study models for hullet decoloration and develor officient localization algorithms that							
15. SUBJECT TERMS							
gunfire localization, time of arrival, angle of arrival, muzzle blast, shock wave, bullet deceleration, fusion							
L P GETT L GET				15. NUME OF PAGES			
u. KEI OKI   0. ADSIKACI   0. IIIISIAGE				OFTAGES	19b. TELEPHONE NUMBER		
UU	UU	UU	UU		570-577-1129		

## **Report Title**

Final Report: Localization of Gunfire from Multiple Shooters (ARO Research Topic 5.2, Information Processing & Fusion; STIR Program)

#### **ABSTRACT**

Soldier-wearable gunfire detection systems (SW-GDS) are important for situational awareness because they provide an estimate of the shooter's location and the trajectory of the bullet. Individual SW-GDS units provide an estimate of the range and bearing to the shooter for each shot, as well as "raw" data that includes time-of-arrival (TOA) and direction-of-arrival (DOA) of the muzzle blast (MB) produced by the weapon and the shock wave (SW) produced by the supersonic bullet. The localization accuracy is improved with data fusion between networked SW-GDS sensor units. We study models for bullet deceleration and develop efficient localization algorithms that explicitly incorporate the deceleration models in the data fusion. Localization algorithms are developed for individual SW-GDS units and fusion of networked SW-GDS units. A statistical analysis of mismatch between the assumed model and actual deceleration is performed, and the localization algorithms are tested with simulations and measured data. The deceleration models and localization algorithms are described in detail in a technical report.

Enter List of papers submitted or published that acknowledge ARO support from the start of the project to the date of this printing. List the papers, including journal references, in the following categories:

(a) Papers published in peer-reviewed journals (N/A for none)

Received Paper

TOTAL:

Number of Papers published in peer-reviewed journals:

(b) Papers published in non-peer-reviewed journals (N/A for none)

Received Paper

TOTAL:

Number of Papers published in non peer-reviewed journals:

(c) Presentations

Number of Presentations: 0.00				
	Non Peer-Reviewed Conference Proceeding publications (other than abstracts):			
Received	<u>Paper</u>			
TOTAL:				
Number of Non	Peer-Reviewed Conference Proceeding publications (other than abstracts):			
	Peer-Reviewed Conference Proceeding publications (other than abstracts):			
Received	<u>Paper</u>			
TOTAL:				
Number of Peer	-Reviewed Conference Proceeding publications (other than abstracts):			
(d) Manuscripts				
Received	<u>Paper</u>			
TOTAL:				

Number of Ma	nnuscripts:		
		Books	
Received	<u>Book</u>		
TOTAL:			
Received	Book Chapter		
TOTAL:			
		Patents Submitted	
		Patents Awarded	
		Awards	
		Graduate Students	
NAME		PERCENT_SUPPORTED	
FTE Ed	quivalent: lumber:		
		Names of Post Doctorates	
NAME		PERCENT_SUPPORTED	
	quivalent: lumber:		

# Names of Faculty Supported NAME PERCENT\_SUPPORTED Richard J. Kozick FTE Equivalent: 0.20 Total Number: 1

# Names of Under Graduate students supported

NAME	PERCENT_SUPPORTED
FTE Equivalent: Total Number:	
This section only applies	Student Metrics to graduating undergraduates supported by this agreement in this reporting period
	er of undergraduates funded by this agreement who graduated during this period: 0.00 ates funded by this agreement who graduated during this period with a degree in science, mathematics, engineering, or technology fields: 0.00
_	es funded by your agreement who graduated during this period and will continue luate or Ph.D. degree in science, mathematics, engineering, or technology fields: 0.00
1	raduating undergraduates who achieved a 3.5 GPA to 4.0 (4.0 max scale): 0.00 g undergraduates funded by a DoD funded Center of Excellence grant for Education, Research and Engineering: 0.00
The number of undergraduates	funded by your agreement who graduated during this period and intend to work for the Department of Defense 0.00
1	tes funded by your agreement who graduated during this period and will receive ips for further studies in science, mathematics, engineering or technology fields: 0.00
	Names of Personnel receiving masters degrees
NAME	

NAME	
Total Number:	
	Names of personnel receiving PHDs
NAME	
Total Number:	

## Names of other research staff

<u>NAME</u>	PERCENT_SUPPORTED	
FTE Equivalent:		
Total Number:		

#### **Inventions (DD882)**

## **Scientific Progress**

A survey of several bullet deceleration models is presented.

For each deceleration model, mathematical expressions are developed that relate the soldier-wearable gunfire detection system (SW-GDS) position and the shooter's position to the measured acoustic data, consisting of time-of-arrival (TOA) and direction-of-arrival (DOA) of the muzzle blast (MB) produced by the weapon and the shock wave (SW) produced by the supersonic bullet. These expressions form the basis for shooter localization algorithms.

In order to exploit SW data for shooter localization, it is necessary to determine the "SW detach range", which the location along the bullet's trajectory at which the SW begins to propagate to the sensor. The SW detach range depends on the bullet deceleration model. We develop efficient algorithms for finding the SW detach range, consisting of closed-form expressions for some deceleration models, and rapidly-converging iterative algorithms for the other deceleration models.

The bullet deceleration model assumed in the localization algorithm may be different than the actual deceleration of the bullet. A statistical analysis of the fusion algorithm is performed to assess the effect of this mismatch in terms of bias and variance of the shooter location estimate.

The "drag force" (DF) bullet deceleration model is the most accurate, based on support from theory and experiments. For the DF model, we provide a complete shooter localization algorithm for individual SW-GDS units as well as a fusion algorithm for networked SW-GDS units.

The performance of the fusion algorithm for shooter localization is evaluated with simulations and field-measured data.

These items are described in detail in a separate document that is submitted as a Technical Report.

**Technology Transfer**